A model of a practical Guanella 1:1 balun

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Abstract

This article presents a model of the Guanella 1:1 balun that reasonably predicts in a single model, in-band performance, and low and high frequency roll off.

1. Guanella’s balun

Guanella described several baluns and ununs in 1944 in his article entitled "New methods of impedance matching in radio frequency circuits".

One particular configuration, the 1:1 balun is of particular interest because of its popularity in various forms in antenna applications.

Figure 1: Guanella's 1:1 balun.

Figure 1 is from Guanella's paper, and it shows his development of the transmission line model for the differential current path, and an inductor for the common mode current path.

This article proposes a lossy transmission line model of a practical Guanella 1:1 balun that is effective for all frequencies within and immediately adjacent to the pass band. The model is of a two wire or coaxial transmission line wound around a toroidal ferrite core, and includes:

• conductor RF resistance including frequency dependent skin and proximity effects;
• transmission line characteristic impedance calculated from conductor RF resistance, dielectric dissipation factor, and including frequency dependent proximity effect; and
• common mode choke impedance calculated from frequency dependent core material $\mu'$ and $\mu''$ or measured R and X vs frequency.

Such a model can be used for exploring not only variations in design such as different core materials, wire thickness and spacing, number of turns etc, but exploration of loads other than the nominally matched balanced load.

2. Equivalent circuit

2.1 Guanella 1:1 balun circuit

Figure 2: Guanella 1:1 balun circuit.

Figure 2 is a Guanella Order-1 Transmission Line Transformer configured as a common mode current choke. Note that the current designations are not related to Guanella's shown in Figure 1.

2.2 Proposed equivalent circuit

Figure 3: Proposed equivalent circuit.

Figure 3 shows the proposed equivalent circuit. The transformers T1 and T2 are ideal transformers that are introduced for the purpose of separating the common...
mode and differential currents. The common mode current is routed through the common mode choke impedance \( Z_c \), and the differential current flows in the transmission line \( T_L \). The common mode current \( I_3 \) is the result of components \( I_3/2 \) which flow into both ends of the left hand winding of \( T_1 \), and out of both ends of the right hand winding of \( T_2 \). The differential mode current can be analysed by transmission line equations, and the common mode current can be analysed by lumped component circuit analysis.

![Figure 4: I3 current path.](image)

Figure 4 shows the I3 current path.

2.3 Solution to equivalent circuit

\[
V_1 = V_2 \cdot \cosh(\theta) + I_2 \cdot Z_0 \cdot \sinh(\theta) \quad \text{(1)}
\]

\[
I_2 = \frac{V_2}{Z_L} \quad \text{(2)}
\]

Substituting (2) into (1):

\[
V_1 = V_2 \cdot \cosh(\theta) + \frac{V_2}{Z_L} \cdot Z_0 \cdot \sinh(\theta) \quad \text{(3)}
\]

\[
\frac{V_1}{V_2} = \frac{\cosh(\theta) + \frac{Z_0}{Z_L} \cdot \sinh(\theta)}{1} \quad \text{(4)}
\]

\[
\frac{V_1}{V_2} = \frac{1}{\cosh(\theta) + \frac{Z_0}{Z_L} \cdot \sinh(\theta)} \quad \text{(5)}
\]

Above is a solution to the proposed equivalent circuit. The quantity \( \theta \) is the product of \( \gamma \), the transmission line complex propagation coefficient, and transmission line length. All other currents, voltages, and powers can be derived from the \( V_2/V_1 \) relationship. Note that quantities in Figure 4 may be complex values, and many are frequency dependent.

Many models of this balun treat \( V_2 \) as equal to \( V_1 \), ie as if \( \theta \) is zero, which is an approximation more valid at low frequencies.

3. A worked example

3.1 Common mode choke

The choke impedance depends on the ferrite core, and its ferrite permeability and loss are frequency dependent.

![Figure 5: Characteristics of #43 mix.](image)

Figure 5 shows the characteristics of Fair-rite #43 mix. The choke impedance cannot simply be modelled as a fixed idealised inductor. The model needs to calculate the equivalent series inductive reactance and loss resistance at each frequency of interest. Choke impedance

\[
Z_c = j \cdot 2 \cdot \pi \cdot f \cdot n^2 \cdot A_l / \mu_{il} f (\mu' - j \mu'')
\]

where \( A_l \) is inductance for 1 turn at \( \mu_r = \mu_{il} f \), and \( \mu_{il} \) is the initial permeability at low frequency.

![Figure 6: Choke impedance.](image)

Figure 6 shows the impedance for a 12 turn choke wound on a Fair-rite 2643801002 (or 5943001001) #43 core (29mmx19mmx7.5mm) calculated from core dimensions and material characteristics and with a parallel capacitance of 1.6pF to calibrate the model to an actual choke. Quantity \( Z_{cm} \) is the magnitude of \( R_{cm} + jX_{cm} \).

Measurement of a choke is likely to be more accurate than estimation from core dimensions, material characteristics and turns. Behavior at high frequency is quite subject to stray capacitance.

3.2 Transmission line

Another challenge is that transmission line \( Z_0 \) and loss may be influenced by both skin and proximity effect. Skin effect causes the current to flow mainly on the surface of conductors, and proximity effect causes currents in
opposite directions to tend to flow mainly on the adjacent surfaces of conductor that are very close together.

Figure 7: Transmission line characteristic impedance.

Figure 7 shows an estimate of Zo based on the log function, the acosh function, and a proximity corrected curve derived from Fig 4.23 of Radio Antenna Engineering by Edmund LaPort, 1952. It would appear that LaPort's graph may be a correction to the log function that he gives in the book, and an estimate of the cosh curve. Neither appear to properly account for proximity effect on Zo. Chipman (Transmission Lines) suggests that the error in Zo due to proximity effect is small for D/d>2 (Zo<160Ω). The acosh curve underestimates Zo for D/d<2 and the error may become significant.

A proximity resistance correction is calculated using an algorithm from the program line_zin.pas by Reg Edwards (G4FGQ).

3.3 Balun performance

Figure 8 shows a plot of VSWR and loss modelled for a Guanella 1:1 balun made with 12 turns of transmission line wound on a Fair-rite 2643801002 (or 5943001001) #43 core (29mmx19mmx7.5mm). The transmission line comprises 0.5mm diameter copper conductors spaced 0.6mm centre to centre. Under matched conditions, losses are very low, 2% at worst. Estimating that the core can probably safely dissipate up to 5W, the balun is probably capable of continuous power rating of 250W.

Figure 6 shows common mode impedance. Common mode impedance is medium to high, which means that this type of balun does offer significant impedance to common mode current, eg on an antenna feed line connected to the balanced port.

4. links

(These articles are now offline, 01/01/2016.)
- A model of the W2DU 1:1 choke balun
- A model of the W2DU 1:1 choke balun using Jaycar LF1258 cores
- A model of the W2DU 1:1 choke balun using Jaycar LF1260 cores
- Model validation - FT240-61-35t

5. Conclusions

Conclusions are:
- there is a quite complex interaction of components in the network;
- many practical components cannot be modelled simply as idealised components;
- the model appears to capture low frequency and high frequency roll-off, and provide a reasonable estimate of VSWR and loss for different load impedances and balance;
- the model needs to include all components that may contribute to performance;
- measurement of a choke is likely to be more accurate than estimation from core dimensions, material characteristics and turns;
- Rules of Thumb (eg that Zo should equal twice the nominal input Z) do not necessarily lead to optimum performance.

6. Changes

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<td>08/02/2008</td>
<td>Initial.</td>
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<tr>
<td>1.02</td>
<td>07/03/2008</td>
<td>Added equivalent self capacitance to model.</td>
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<tr>
<td>1.03</td>
<td>04/04/2008</td>
<td>Typo corrected.</td>
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<td>1.04</td>
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